# Statistical tensile strength of Nextel<sup>™</sup> 610 and Nextel<sup>™</sup> 720 fibres

D. M. WILSON

3M Metal Matrix Composites Department, St. Paul, MN 55144-1000 USA

The properties of fibre-reinforced composites are dependent not only on the strength of the reinforcement fibre but also the distribution of fibre strength. In this study, the single filament strength of several lots of Nextel<sup>™</sup> 610 and Nextel<sup>™</sup> 720 ceramic fibres was measured. Fracture statistics were correlated with the effects of gauge length and diameter variation, and the Weibull modulus was calculated using several different techniques. It was found that the measured Weibull modulus at a single gauge length did not accurately predict either the gauge length or diameter dependence of tensile strength.

## 1. Introduction

Two new polycrystalline fibres, Nextel<sup>TM</sup> 610 and Nextel<sup>TM</sup> 720 fibre, have recently become commercially available. (At this time, both types of fibre are experimental products.) Nextel<sup>TM</sup> 610 fibre is an alpha-alumina fibre with excellent strength and high elastic modulus. Tensile strengths for polycrystalline fibres above 3 GPa had previously only been achieved by SiC fibres. Oxide fibres have superior resistance to oxidation and corrosion in certain environments; because of this, oxide fibres have the potential to produce composites with unique and superior properties. For instance, the high strength of Nextel<sup>TM</sup> 610 fibre has allowed the development of a new generation of aluminum matrix composites which have tensile strength in excess of 1500 MPa [1]. In addition, oxide fibres are produced from aqueous solutions or sols, and are fired in air, which makes them less expensive than SiC fibres. Nextel<sup>TM</sup> 720 fibre was developed with the goal of maximizing creep resistance. The creep resistance of Nextel<sup>TM</sup> 720 fibre is higher than other polycrystalline oxide fibre, and allows the fabrication of composites with useful mechanical properties at 1100 °C or above. Both Nextel<sup>TM</sup> 610 and 720 fibres have excellent chemical stability due to their high alumina content and crystalline nature. A summary of the properties of Nextel<sup>TM</sup> 610 and 720 fibre are given in Table I. The microstructure and high temperature properties of both fibres have been described previously [2, 3, 4].

Nextel<sup>TM</sup> 610 and 720 fibres are specifically targeted as reinforcements for metal and ceramic composites. The strength of metal and ceramic composites is critically dependent on not only the strength but the strength distribution of the reinforcing fibre. Thus, a thorough understanding of fibre mechanical properties is of prime importance. The purpose of this study is to describe the tensile strength and statistical distribution of tensile strength of Nextel<sup>TM</sup> 610 and 720 fibres.

The statistical variability of the tensile strength of reinforcement fibres is now commonly reported in terms of Weibull modulus. An excellent review of the subject was given by Van der Zwaag [5]. The Weibull modulus is a parameter used to describe the distribution of strength in materials which break at defects according to weakest link statistics. The probability of failure of a material is given by

$$P = 1 - \exp[-(V/V_0)(\sigma/\sigma_0)^m]$$
 (1)

where m = Weibull modulus, V = tested volume,  $\sigma =$  failure strength,  $V_0$ ,  $\sigma_0 =$  scaling constants.

By rearranging and taking the natural logarithm of both sides of the equation, the following equation is obtained

$$\ln [\ln(1/1 - P)] - \ln (V/V_0) = m \ln \sigma - m \ln \sigma_0 (2)$$

The Weibull modulus, m, is typically determined graphically by one of two methods. For a constant tested volume (gauge length for fibres), Equation 2 is reduced to

$$n\left[\ln\left(1/1 - P\right)\right] = m\ln\sigma + k \tag{3}$$

where k is a constant. The Weibull modulus can be determined by plotting  $\ln [\ln (1/1 - P)]$  against  $\ln \sigma$ . Alternatively, m can be determined from the gauge length dependence of strength. If we hold the fracture probability P constant by measuring mean strength, then Equation 2 reduces to

$$\ln \sigma = -1/m \ln V + k' \tag{4}$$

or, alternatively

1

$$\sigma_1/\sigma_2 = (V_2/V_1)^{1/m}$$
 (5)

where the strength at tested volumes  $V_1$  and  $V_2$  are  $\sigma_1$  and  $\sigma_2$ , respectively, and k' is a constant. Since the tested volume is proportional to gauge length, the Weibull modulus m can be determined by plotting mean strength as a function of gauge length. The slope of such a plot is equal to -1/m. This method of measuring Weibull modulus is attractive because the composite designer is interested in the strength of the fibre at the "ineffective length", or length at which

TABLE I Nextel<sup>™</sup> 610 and 720 fibre properties

	Nextel <sup>TM</sup> 610	Nextel <sup>TM</sup> 720
Composition (wt %)	99% Al <sub>2</sub> O <sub>3</sub>	85% Al <sub>2</sub> O <sub>3</sub> + 15% SiO <sub>2</sub>
Crystal structure	$\alpha$ -Al <sub>2</sub> O <sub>3</sub>	$\alpha$ -Al <sub>2</sub> O <sub>3</sub> + mullite
Elastic modulus (GPa)	380	260
Diameter (µm)	11.5	12.5
Density (g cm <sup>-3</sup> )	3.9	3.4
Creep rate (1/s)	$1 \times 10^{-7}$	$< 1 \times 10^{-10}$
(1100 °C/70 MPa)		

the matrix transfers the load to the fibre in shear within the composite. The ineffective length is typically very small, perhaps a few hundred micrometres in most composite systems. Thus, extrapolating the gauge length dependence of strength to short gauge length should produce the most accurate estimation of composite strength.

To consider the effects of fibre diameter, Equation 1 can be expanded to

$$P = 1 - \exp[-(\pi/4) LD^2 / V_0 (\sigma/\sigma_0)^m] \quad (6)$$

where D is the fibre diameter and L is gauge length. By an analogous method to Equation 2

$$\ln [\ln(1/1 - P)] = \ln (\pi/4) L/V_0 + 2 \ln D + m \ln \sigma - m \ln \sigma_0$$
(7)

Therefore, for a constant gauge length

$$\ln \sigma = -2/m \ln D + k'' \tag{8}$$

Thus, a graph of  $\ln \sigma$  versus  $\ln D$  should have a slope of -2/m.

Another useful and simple equation for estimating Weibull modulus is [6]

$$m = 1.2/CV \tag{9}$$

where CV is coefficient of variation of strength at a single gauge length. This estimation is very accurate for m > 10. For instance, for a CV of 0.10, m is estimated to be 12.

#### 2. Experimental procedure

Single filament strength testing was performed using rubber-faced clamp grips with  $25 \times 25$  mm grip faces. For Nextel<sup>TM</sup> 610 fibre, this method was found to give higher breaking loads than paper tabs recommended in ASTM-3379-75. The tested gauge length was 25 mm unless otherwise specified, and the strain rate was  $0.02 \text{ min}^{-1}$ . In this study, almost no fibres were lost due to breakage during sample mounting and testing. Achieving good alignment of fibres with the grips and load axis was critical to obtaining accurate load values.

During fibre testing, no fibre remained in the gauge length after fracture. It is believed that this resulted from vibrations caused by the release of stored strain energy during fibre fracture. Therefore, fibre diameter was measured on fibre ends removed from the grips after fibre failure. Scanning electron microscopy (SEM) examination (Cambridge 240) found that fibre of individual fibres within 25 mm length. Thus, fibre diameter in the grips is expected to be equal to the diameter at the point of fracture. In this work, fibre diameter was measured using a Measure-Rite<sup>TM</sup> image analysis system (Model M25-6002, Dolan-Jenner Industries) attached to a light microscope (Olympus<sup>TM</sup> BHS) at  $1000 \times$  magnification. Prior to this study, a number of fibre diameter measurement methods, including unaided optical microscopy, laser diffraction/refraction and vibroscopes were evaluated. Significant variability was found in all in comparison to SEM measurements. The image analysis system was found to provide the most accurate diameter measurements and was also simple to use, a significant factor in minimizing operator fatigue and maintaining measurement accuracy. In this system, fibre ends were measured relative to a round template on a video monitor. Blind, replicate studies were performed to determine measurement accuracy. The image analysis method was repeatable to an average error of  $< 0.1 \,\mu$ m, and the mean difference between testers was also  $< 0.1 \,\mu\text{m}$ . In these tests, diameter values measured using this technique were between 0.0 and 0.3 µm less than SEM measurements (standardized relative to a 10 µm SEM calibration grid). The reason for this difference is unknown. The image analysis system was consistently accurate to  $< 0.1 \,\mu\text{m}$  in measuring the calibration grid. Thus, reported tensile strength may be as much as 5% higher (  $\sim 28$  MPa) than true values. Diameter measurements correlated to within 1% (0.12  $\mu$ m) of diameters calculated from measured fibre density and weight per unit length.

diameter was constant within 0.1 µm down the length

In this study, several production lots of fibre were tested. Fibres were taken from several spools throughout each lot to incorporate any possible property variation within the lot in fibre fracture statistics. For each spool tested, the strength of ten single filaments were measured. Using this data, Weibull modulus was calculated using three methods: (i) Weibull plot, or strength distribution, method (Equation 3), (ii) gauge length method (Equation 4) and (iii) diameter method (Equation 8). For Weibull plots, P = (i - 0.5)/n was used to estimate fracture probability, where *n* is the number of fibres tested and *i* is the rank of strength for each fibre. This is the most accurate estimator for small sample sizes [7, 8].

#### 3. Results

### 3.1. Classical Weibull statistical analysis

Table II shows a data series for Nextel<sup>TM</sup> 610 and 720 fibres. The measured strengths are typical of fibres currently being produced. The mean breaking loads of these lots were 3077 and 1964 MPa, respectively. The strength of Nextel<sup>TM</sup> 610 fibre is higher, primarily because of its finer grain size. The diameter of Nextel<sup>TM</sup> 720 fibre is slightly larger, 12.5  $\mu$ m compared with 11.5  $\mu$ m for Nextel<sup>TM</sup> 610 fibre. The coefficient of variation of diameter of both fibres is small, less than 5%. Fig. 1 shows the distribution of single filament strength for three lots of Nextel<sup>TM</sup> 610 fibre. For individual lots, approximately 80% of the fibres broke

TABLE II Nextel <sup>™</sup> 6	510	and	720	fibre	tensile	data
--------------------------------	-----	-----	-----	-------	---------	------

Nextel <sup>TM</sup> 610 fibre (A0168)		Nextel <sup>TM</sup> 720 fibre (A0172)			
Load (g)	Fibre diameter (μm)	Strength (MPa)	Load (g)	Fibre diameter (µm)	Strength (MPa)
28.5	11.0	2944	26.4	12.3	2199
32.8	11.3	3206	26.3	12.3	2185
32.3	12.1	2751	22.6	12.3	1882
31.6	11.3	3089	23.3	11.1	2358
33.0	11.0	3406	22.5	11.1	2282
32.9	11.2	3275	24.6	11.6	2282
27.6	11.5	2606	26.4	12.3	2192
29.3	11.6	2723	21.4	12.4	1744
25.3	11.3	2475	23.1	11.8	2061
28.9	11.1	2930	21.1	12.6	1648
26.8	11.5	2530	26.6	12.1	2261
27.2	11.9	2399	20.1	12.4	1641
33.4	12.2	2806	22.3	12.1	1896
32.1	11.9	2827	24.1	12.5	1923
30.2	11.3	2951	21.0	11.9	1861
26.2	10.7	2854	23.9	12.5	1903
28.4	11.0	2930	21.5	12.0	1868
25.8	11.2	2565	16.6	12.0	1441
27.6	11.1	2799	23.7	11.9	2096
30.1	11.0	3102	26.6	12.3	2213
36.6	11.5	3454	22.9	12.9	1717
40.6	11.0	4185	25.5	12.7	1972
35.1	11.9	3095	22.1	12.9	1655
29.2	10.6	3247	22.8	13.0	1682
30.9	10.7	3371	27.6	12.5	2206
34.4	11.4	3302	21.5	12.5	1641
36.2	11.4	3544	19.2	12.0	1462
38.5	11.5	3454	15.2	12.0	1734
39.3	11.0	3468	20.9	13.5	1434
35.5	11.7	3233	31.4	12.7	2434
32.2	12.5	2571	23.1	11.8	2454
29.4	10.6	3268	10.1	11.0	1868
22.4	11.3	2792	22.3	12.0	1937
20.0	12.0	2016	26.0	13.1	1058
20.7	12.0	3006	20.9	12.1	2206
22.7	10.0	3523	23.7	12.1	2158
26.6	10.9	2058	24.1	11.0	2138
20.0	10.0	3123	25.4	11.5	2468
29.7	10.9	2930	10.1	11.5	1841
25.1	10.7	2530	19.8	11.0	1834
3/0	11.0	3075	24.6	12.7	1003
33.5	11.9	3337	24.0	12.7	2179
33.5	11.2	3468	20.0	12.2	1000
30.4	10.8	3254	20.0	12.7	1641
20.5	10.8	3254	20.9	12.0	2165
39.5	12.7	2647	20.7	12.4	2105
32.2 20.1	10.5	2205	10.8	15.0	2303
29.1	10.5	3293	19.0	11.5	1000
22.1	11.5	2971	10.2	11.7	1648
33.I 21.5	11.0	3008	19.5	12.1	1048
31.5	10.8	33/1	26.8	12.4	2179
Mean					
31.5	11.3	3077	23.5	12.2	1964
SD					
3.88	0.52	348	3.46	0.56	287
CV					
0.123	0.046	0.113	0.147	0.045	0.146

within 10% of the mean strength, indicating a high degree of consistency between fibres. The data has a sinusoidal form, as expected. Lot A0184 had the highest mean tensile strength of any lot tested to date, 3500 MPa. Lots A0168 and A0180 were more typical, having tensile strength near 3000 MPa. Weibull plots



*Figure 1* Fracture probability of three lots of Nextel<sup>TM</sup> 610 fibre. ( $\blacktriangle$ ) A0168; ( $\bigcirc$ ) A0180; ( $\diamondsuit$ ) A0184.



*Figure 2* Weibull plot for three lots of Nextel<sup>TM</sup> 610 fibre. (○) A0168, mean = 3080, m = 10.9; (♥) A0180, mean = 3030, m = 11.2; (△) A0184, mean = 3500, m = 12.1.

TABLE III Weibull properties of Nextel<sup>™</sup> 610 fibre

Lot	Mean strength (MPa)	Weibull Modulus Calculation			
		Strength distribution	Diameter distribution	Gauge length dependence	
A0168	3080	10.9	2.7	_	
A0180	3030	11.2	2.6	-	
A0184	3500	12.1	4.0	_	
Mean	3200	11.4	3.1	21.7	

for the three lots of Nextel<sup>TM</sup> 610 fibre are shown in Fig. 2. The calculated Weibull modulus varied between 10.9 and 12.1 for the three lots (Table III). The data was fitted using the least squares method; the two-parameter Weibull equation fit the data fairly well, although some deviation of from the best-fit line occurred at the high and low strength extremes. The Weibull modulus calculated using the strength distribution technique (Equation 3) for all three lots of fibre was 11–12. The corresponding strength distribution



*Figure 3* Fracture probability of two lots of Nextel<sup>TM</sup> 720 fibre. ( $\bigcirc$ ) A0174; ( $\blacklozenge$ ) A0080.



*Figure 4* Weibull plot for two lots of Nextel<sup>TM</sup> 720 fibre. ( $\bigcirc$ ) A0174, mean = 2030, *m* = 8.1; ( $\blacktriangle$ ) A0080, mean = 2130, *m* = 7.1.

TABLE IV Weibull properties of Nextel<sup>TM</sup> 720 fibre

Lot	Mean strength (MPa)	Weibull Modulus Calculation			
		Strength distribution	Diameter distribution	Gauge length dependence	
A0080	2130	7.1	4.0	_	
A0174	2030	8.1	1.6	26.4	
Mean	2080	7.6	2.8	-	

and Weibull plot for Nextel<sup>TM</sup> 720 fibre is given in Figs 3 and 4. The tensile strength of Nextel<sup>TM</sup> 720 fibre was less than that of Nextel<sup>TM</sup> 610 fibre, ranging from 1500 to 2700 MPa. The Weibull modulus for Nextel<sup>TM</sup> 720 fibre was also less than for Nextel<sup>TM</sup> 610 fibre, approximately 7.1 and 8.1 for lots A0080 and A0174, respectively (Table IV).

#### 3.2. Gauge length effects

The mean tensile strength of four lots of Nextel<sup>TM</sup> 610 fibre and one lot of Nextel<sup>TM</sup> 720 fibre as a function of



*Figure 5* Tensile strength of four lots of Nextel<sup>TM</sup> 610 fibre as a function of gauge length. The line is the least squares fit of the mean strength of all four lots. ( $\bigcirc$ ) A0175; ( $\times$ ) A0178; ( $\bigcirc$ ) A0182; ( $\triangle$ ) A0184.



*Figure 6* Tensile strength Nextel<sup>TM</sup> 720 fibre as a function of gauge length (A0174, m = 26.4).

gauge length is given in Figs 5 and 6, respectively. Ten filaments were measured for each data point. For Nextel<sup>TM</sup> 610 fibre, the scatter in the data was large enough that the mean strength for all four lots was used to calculate Weibull modulus. For both types of fibre, the reduction of strength with increasing gauge length was small. For Nextel<sup>TM</sup> 610 fibre, mean fibre strength decreased only 10% (from 3080 to 2780 MPa) for a 10-fold increase in gauge length. For some individual lots, the measured tensile strength actually increased with gauge length. This amount of variability was not surprising, since the coefficient of variation in mean tensile strength averaged about 0.1 or 10% for these fibres, equal to the variation in strength over the gauge length tested. Using the mean strength, the Weibull modulus for Nextel<sup>TM</sup> 610 and Nextel<sup>TM</sup> 720 fibre were 22 and 26, respectively. This is substantially higher than the Weibull modulus measured from the distribution of tensile strength.

## 3.3. Diameter effects

Commercial ceramic fibres do not have a completely uniform diameter throughout all fibres in a bundle or



*Figure 7* Tensile strength of three lots of Nextel<sup>TM</sup> 610 fibre as a function of fibre diameter. ( $\bigcirc$ ) A0168; (+) A0180; ( $\blacktriangle$ ) A0184.



*Figure 8* Tensile strength of Nextel<sup>TM</sup> 720 fibre as a function of fibre diameter. ( $\bigcirc$ ) A0080; ( $\blacklozenge$ ) A0174.

tow. Because diameter varies from fibre to fibre, testing fibres at constant gauge length does not maintain a constant tested volume. The distribution of volumes is proportional to the distribution of fibre diameters.

The natural log of tensile strength as a function of the natural log of fibre diameter for Nextel<sup>TM</sup> 610 and Nextel<sup>TM</sup> 720 fibre is plotted in Figs 7 and 8, respectively. As given in Equation 8, the slope of the best fit line is equal to -2/m. For Nextel<sup>TM</sup> 610 fibre, the Weibull modulus calculated using this data for all three lots was between 2.6 and 4. The scatter in this data was large; however, the trend was very consistent. A large amount of scatter is expected due to the statistical nature of fracture. The trend was also similar for other data not presented here; thus, the result is believed to be reliable despite the scatter. For Nextel<sup>TM</sup> 720 fibre, the Weibull modulus was 4.0 and 1.6 for lots A0080 and A0174, respectively. For both Nextel<sup>TM</sup> 610 and 720 fibres, this value was much lower than determined using the other methods. In both cases, the low m indicated a stronger dependence of strength on diameter than the gauge length

measurements. Tables III and IV summarize the Weibull modulus results using all analysis methods.

#### 4. Discussion

The tensile strength of Nextel<sup>TM</sup> 610 fibre is by far the highest strength measured for any polycrystalline oxide fibre. Other commercially available oxide fibres have reported tensile strengths of no more than 2.1 GPa [9]. Early lots of Nextel<sup>TM</sup> 610 fibre (pre-1993) had tensile strengths near 2.5 GPa, better than other commercial materials, but lower than target properties for metal-matrix composite (MMC) reinforcements. Fractography experiments on early versions of Nextel<sup>TM</sup> 610 fibre identified several types of fracture origins, including internal inclusions caused by both inorganic and organic particulate contamination, surface welding and other surface damage [10]. Process development work targeted the elimination of these flaws as a method of increasing fibre strength. These efforts were successful; improvements in process cleanliness during precursor preparation and improved fibre processing techniques since that time have resulted in significantly increased single filament strength.

The measured Weibull modulus of Nextel<sup>TM</sup> 720 fibre and especially, Nextel<sup>TM</sup> 610 fibre was also much higher than most multifilament ceramic fibres. For instance, Weibull moduli for Nicalon are 3–4 [11–13], Fiber FP 4–6 [12–16], Altex 4–6 [17, 18] and carbon fibres 3-8 [19-22]. For early lots of Nextel<sup>TM</sup> 610 fibres, it was also found that the Weibull modulus was below 10 [23]. As process development work eliminated large flaws and increased tensile strength, the Weibull modulus also increased. This is not surprising, since eliminating large flaws from a population of defects will leave only the small flaws remaining. This would narrow the flaw size distribution, resulting in increased Weibull modulus. Fractography experiments also confirmed that flaw size for recent lots was reduced compared with earlier, weaker fibres. The correlation between high fibre strength and high Weibull modulus has been noted previously [5].

The three Weibull modulus measurement techniques investigated in this study produced very different results. For both Nextel<sup>TM</sup> 610 and Nextel<sup>TM</sup> 720 fibres, the calculated Weibull modulus was much higher with the gauge length method than with the Weibull plot method, which was in turn much higher than the diameter method. Thus, it is clear that the simple two-parameter Weibull model does not describe the tensile strength statistics of either fibre. Specifically, the Weibull modulus determined from the statistics of fracture at one gauge length cannot be used to determine strength at other gauge lengths or for fibres with different diameters. An examination of the literature for ceramic fibres finds that large differences in Weibull modulus for the gauge length and strength distribution technique are common. The Weibull modulus has been determined to be a factor of two higher with the gauge length technique than the strength distribution technique for Fiber FP and PRD-166 [15], Nicalon [13], and carbon fibres [24, 25]. The reason for this phenomenon is not fully understood. However, some speculation on possible causes may be useful.

It is not commonly understood that fibre diameter variability will have an effect on measured Weibull modulus. Weibull theory predicts that fibres with larger diameter should, on average, have a greater chance to have a large flaw, and will therefore be weaker than smaller fibres. This is well understood. However, for fibre testing, it has special relevance. Because there is a distribution of individual fibre diameters within a tow, the tested volume will vary even when the tested gauge length is constant. Thus, the measured strength distribution will be created by the overlap of the dispersion of strength due to the volumetric distribution of flaws and due to the variable fibre volume. Because of this effect, the natural distribution of fibre strength will be artificially broadened, lowering the measured Weibull modulus. Initially, it was suspected that the measured Weibull modulus of 12 for Nextel 610<sup>TM</sup> fibres at 25 mm gauge length could have resulted from the combined effect of a gauge length Weibull modulus of 22 with a diameter Weibull modulus of 3. To determine the viability of this hypothesis, a few simple calculations were made. The width of overlapping distributions can be calculated using the following equation

$$CV_{\text{total}}^2 = CV_1^2 + CV_2^2 \tag{10}$$

where  $CV_1$  and  $CV_2$  are the coefficient of variations of populations 1 and 2, respectively. For Nextel 610<sup>TM</sup> fibres, the coefficient of variation in fibre diameter was 0.046. This is equivalent to a 9.4% variation in volume. For a Weibull modulus (relative to diameter variation) of 3, Equation 5 predicts a change in strength of 3.0% for a 9.4% change in volume. For m = 22, the CV will be 0.0545 (from Equation 9). Combining the CVs with Equation 10, the measured CV would be  $(0.0545^2 + 0.03^2)^{1/2} = 0.0624$ , equivalent to m = 19.2. This is a change of 13% from the "true" value of 22. However, it does not accurately predict the measured value of 12. Therefore, this effect does not explain the observed results. Note, however, that this effect could become quite important if the diameter variability were larger. The diameter distributions of other ceramic fibres can be as much as 15% [9, 13]. For a diameter CV of 0.15, the combined Weibull modulus using m = 3 and 22, as above, would be  $(0.0545^2 + 0.0976^2)^{\frac{1}{2}} = 0.112$ . This is equivalent to m = 10.7, or only about 50% of the "true" Weibull modulus. This is a significant change.

An initial attempt to treat this effect analytically was made by Wagner [26, 27]. A three-parameter model for Weibull modulus using an additional parameter  $\delta$  to take into account the effect of fibre diameter was proposed

$$P = 1 - \exp[-(D/D_0)^{\delta}(\sigma/\sigma_0)^m]$$
(11)

where  $\delta$  is a parameter similar to Weibull modulus and  $D_0$  is a scaling parameter. Wagner assumed that the parameter  $\delta$  was equal to 2/m, as predicted by the Weibull equations for volume flaws. This equation was also used by Masson [20]. In that study,  $\delta$  was allowed to take any value; it was found that  $\delta$  was typically as large or larger than *m*, but the scatter was also large. However, in both cases, Equation 10 was found to provide improved fit to the experimental data. Potentially, this equation could be extended to gauge length variation as well, with a third experimental parameter. However, this would add considerable complication to the Weibull theory. Because of this, and since these effects were not large enough to explain the results with Nextel fibres, no attempt was made to calculate  $\delta$  in this study.

Diameter measurement error could also produce significant changes in measured Weibull modulus. If, because of measurement errors, some fibres are measured to have smaller diameters than they actually have, erroneously high strength values will be generated. Conversely, erroneously large diameter measurements will produce low strength values. Thus, the consequence of this phenomenon is that the strength distribution at a single gauge length will be broadened, so the Weibull modulus will be underestimated. For instance, a mean diameter measurement error of 5% would produce a CV in area and therefore measured strength, of 10.25%. Using Equation 9, a CV in strength of 0.1025 corresponds to a Weibull modulus of 11.7. Thus, even if the fibre had zero true variability, the Weibull modulus would be less than that measured for Nextel 610. Note that a 5% error in diameter measurement represents only 0.6 µm for a 12 µm diameter fibre. Given that most fibre diameter measurements are done using optical microscopes, this magnitude of error would not be unexpected, unless special precautions are taken. Thus, extreme care must be taken to minimize diameter measurement error. In this study, the measurement error was 0.1%. This would produce a CV in strength of 0.0175. If the true Weibull modulus was 22, the combined CV would be  $(0.0545^2 + 0.0175^2)^{1/2} =$ 0.0572, equivalent to m = 21.0. This is only 5% less than the Weibull modulus in the absence of measurement errors. Therefore, measurement error is not sufficient to explain the observed differences in Weibull modulus.

If we assume that measurement error is not a factor, and diameter variability is not large enough to explain the differences in measured Weibull modulus, then what physical phenomenon could cause the Weibull modulus to be largest with respect to gauge length variability, intermediate for the strength distribution, and smallest for the diameter variability? This result suggests that the flaw population is not random, but that (i) there are, on average, larger flaws in large diameter fibres than predicted from their increased volume, and (ii) there is a broader flaw distribution between different fibres in a tow than the distribution of flaws down the length of a single fibre. Considering situation (i), there are several reasons why fibre diameter would be expected to have a stronger than predicted effect on strength than gauge length. Experiments with large diameter Nextel<sup>TM</sup> 610 fibres for titanium and intermetallic composites have demonstrated that it is difficult to produce large diameter fibres using the Nextel<sup>TM</sup> process. High strength continuous fibres with diameters as large as  $20 \,\mu$ m have been produced [28], but significant process changes were required. If these processes are not performed correctly, critical defects, such as welds, blisters and voids, were created during processing. In a single tow, all fibres are processed at identical conditions. Thus, the larger fibres in the tow may have a larger probability of incurring process-related damage than the smaller fibres. This would produce the low Weibull modulus as measured by the diameter variability method. However, note that the observed flaws in these fibres were primarily welds, which are not related to pyrolysis problems (see below).

Situation (ii), the prediction of variation in flaw population between different fibres, is illustrated in Fig. 9. In this scenario, each fibre would have a separate and unique population of flaws. Some fibres would have a distribution of relatively small flaws. Some fibres would have a distribution of larger flaws. Thus, if one separated a number of fibres from the bundle and tested them, one would get a wide strength distribution (and therefore low Weibull modulus), since the flaw size on different fibres would be quite different. However, if one tested fibres at different gauge lengths, the result would be a high Weibull modulus. This is true since this measurement would not be related to the distribution of flaw size between fibres, but would correspond to the distribution of flaws within individual fibres. The wide strength distribution between fibres would be lost, since the mean strength at each gauge length, rather than the distribution of strength, would be used for the analysis. The Weibull modulus, as determined from the strength distribution at a single gauge length, would have an intermediate value. This physical model would explain the observed results for Nextel<sup>™</sup> 610 and 720 fibres.

The question then arises: is there a plausible physical basis for this scenario? The most common cause of fracture in Nextel<sup>TM</sup> 610 and 720 fibres are weld lines. Fig. 10 shows a Nextel<sup>TM</sup> 610 fibre with fracture originating at a weld line (fracture stress = 2960 MPa). These are believed to result from contact between adjacent fibres during processing, possibly during sintering. The size of the flaws is typically  $< 0.5 \,\mu\text{m}$ , as expected by simple calculation from the Griffith fracture criterion using  $K_{Ic} = 4$  for alumina. For fibres to form welds, they must obviously be in contact with adjacent fibres. In a tow of 420 filaments, it would be expected that some filaments would be touching and some would not. For instance, the opportunities for fibres on the outside of the tow to touch neighbours is less than in the centre of the bundle. The severity of the weld would then vary between fibres within a bundle. Conversely, the weld line may produce a very narrow distribution of flaws down the length of the fibre. Of course, for any given fibre, the weld tracks may start and stop at various points down the length of the fibre. However, within the gauge length examined in this study, welding may be consistent down the length of the fibre. Thus, it seems possible that the scenario of Fig. 9 may occur.

In earlier generation Nextel<sup>TM</sup> 610 fibres, in addition to lower Weibull modulus, the gauge length



*Figure 9* Schematic flaw size distributions. Some fibres have larger flaws than others, but the size distribution is narrow for individual fibres.



Figure 10 Scanning electron micrograph of Nextel<sup>TM</sup> fibre showing weld line at fracture origin.

and standard deviation methods produced equal results [10]. However, this fibre had a different type of fracture origin [29]. Although welds were also observed, particulate inclusions originating as contaminants in the fibre precursor were a primary cause of fracture. In this case, defects would be expected to be distributed randomly in the volume of the fibres, since each particle would have an equal chance of being incorporated into any fibre. This creates a situation where the Weibull theory, which assumes a random distribution of flaws within the volume of the samples, is accurate. Thus, even for a single fibre type such as Nextel<sup>TM</sup> 610, it is difficult to have a high degree of confidence in extrapolating Weibull parameters without extensive test data, including a detailed knowledge of the fracture origins. Perhaps it is not surprising that the fracture statistics change with process modifications; however, this illustrates the difficulty in using Weibull theory for mechanical property prediction. Certainly, using Weibull theory without considering the nature of the flaw distributions can lead to an incorrect extrapolation of fibre properties.

## 5. Conclusions

The tensile strength of Nextel<sup>TM</sup> 610 and Nextel<sup>TM</sup> 720 fibres was determined to be 3200 and 2100 MPa, respectively. The high strength and narrow strength distribution of Nextel<sup>TM</sup> 610 was attributed to a reduction in flaw size due to process improvements.

The Weibull modulus of both fibres was measured using three different techniques. The Weibull modulus of Nextel<sup>TM</sup> 610 and Nextel<sup>TM</sup> 720 fibres was 22 and 26, respectively, when determined from the variability with changing gauge length, 11.5 and 8, respectively, when determined from strength variability at a single gauge length, and 3.1 and 2.8, respectively, when determined from variability between fibres with different diameters. Thus, traditional two-parameter Weibull statistics were not sufficient to describe the fracture statistics of Nextel<sup>TM</sup> 610 and Nextel<sup>TM</sup> 720 fibres. Mechanisms for non-random fibre flaw generation during fibre processing were proposed to explain the measured effects.

The high Weibull modulus with respect to strength variability and gauge length variation indicates the degree of consistency achieved during fibre processing. The effect of the low Weibull modulus with respect to diameter variation is of minor practical importance because the diameter size variability was small.

# Acknowledgements

The assistance of Dave Lueneburg, Steve Lieder, and Margaret Vogel-Martin in fibre test development as well as Dave Jensen and Robinson Vo at 3M and Alan Seid and Christy Schramm at Touchstone Research Laboratories in fibre testing is gratefully appreciated.

## References

- 1. H. E. DEVE and C. McCULLOUGH, J. Metals. 47 (1995) 33.
- 2. D. M. WILSON, D. C. LUENEBURG and S. L. LIEDER, Ceram. Eng. Sci. Proc. 14 (1993) 609.

- D. M. WILSON, S. L. LIEDER and D. C. LUENEBURG, in Materials Research Society Symposium Proceedings, Vol. 350, Intermetallic Matrix Composites III, edited by J. A. Graves, R. R. Bowman and J. J. Lewandowski (Materials Research Society, Pittsbury, PA, 1994) p. 89.
- 4. Idem., Ceram. Eng. Sci. Proc. 16 (1995) 1005.
- 5. S. VAN DER ZWAAG, J. Test Eval. 17 (1989) 292.
- 6. A. KELLY and N. H. MACMILLAN, "Strong solids", 3rd ed. (Clarenden Press, Oxford, 1986).
- 7. B. BERGMAN, J. Mater. Sci. Lett. 5 (1986) 611.
- 8. J. K. WEDDELL, J. Text. Inst. 81 (1990) 333.
- 9. B. BERGMAN, J. Mater. Sci. Lett. 3 (1984) 689.
- M. M. VOGEL-MARTIN and D. M. WILSON, in Proceedings of 16th Annual Conference on Metal Matrix Carbon and Ceramic Matrix Composites (NASA Conference Publication 3175, part 2, 1992) p. 519.
- 11. H. F. WU and A. N. NETRAVALI, J. Mater. Sci. 27 (1992) 3318.
- 12. Y. MATSUO, J. X. LI and S. KIMURA, *Adv. Comp. Mater.* **2** (1992) 17.
- 13. G. SIMON and A. R. BUNSELL, J. Mater. Sci. 19 (1984) 3649.
- 14. J. NUNES, Comp. Technol. Rev. 5 (1983) 53.
- 15. V. LAVASTE, J. BESSON and A. R. BUNSELL, J. Mater. Sci. 30 (1995) 2042.
- 16. S. N. PATANKAR, J. Mater. Sci. Lett. 10 (1991) 1176.
- 17. Ch. LESNIEWSKI, C. AUBIN and A. R. BUNSELL, *Comp. Sci. Technol.* **37** (1990) 63.
- 18. K. JAKUS and V. TULLURI, *Ceram. Eng. Sci. Proc.* **10** (1989) 1338.
- Y. TANABE, E. YASUDA, A. R. BUNSELL, Y. FAVRY, M. INAGAKI and M. SAKAI, J. Mater. Sci. 26 (1991) 1601.
- 20. J. J. MASSON, K. SCHULTE, F. GIROT and Y. LE PETITCORPS, *Mater. Sci. Eng.* A135 (1991) 59.
- 21. S-H. OWN, R. V. SUBRAMANIAN and S. C. SAUNDERS, J. Mater. Sci. 21 (1986) 3912.
- 22. J. BREEDON JONES, J. B. BARR and R. E. SMITH, J. Mater. Sci. 15 (1980) 2455.
- 23. Z. R. XU, K. K. CHAWLA and X. LI, *Mater. Sci. Eng.* A171 (1993) 249.
- 24. El. M. ASLOUN, J. B. DONNET, G. GUILPAIN, M. NAR-DIN and J. SCHULTZ, J. Mater. Sci. 24 (1989) 3504.
- 25. J. W. HITCHON and D. C. PHILLIPS, *Fiber Sci. Technol.* **12** (1979) 217.
- 26. H. D. WAGNER, S. L. PHOENIX and P. SCHWARTZ, *J. Comp. Mater.* **18** (1984) 312.
- 27. H. D. WAGNER, J. Poly. Sci.: Part B: Polym. Phys. 27 (1989) 115.
- 28. M. A. LEITHEISER and D. M. WILSON, Alumina Fiber Development NASP Materials/Structures Maturation Program, Phase II Final Report, February, 1991.
- D. M. WILSON, in Proceedings of the 14th Annual Conference on Metal Matrix Carbon and Ceramic Matrix Composites, January 1990, edited by J. Buckley NASA Conference Proc. 3097, Part 1, p. 105.

Received 23 July and accepted 23 October 1996